

Statistical Modeling for Radiation Hardness Assurance

Ray Ladbury
Radiation Effects and Analysis Group
NASA Goddard Space Flight Center





BJT—Bipolar Junction Transistor

CL—Confidence Level

DSEE—Destructive SEE

JFET—Junction Field Effect Transistor

MOSFET—Metal-Oxide-Semiconductor Field Effect Transistor

RLAT—Radiation Lot Acceptance Test

SEB—Single-Event Burnout

SEE—Single-Event Effect

SEGR—Single-Event Gate Rupture

SEL—Single-Event Latchup

SOI—Silicon on Insulator

TID—Total Ionizing Dose

RPP—Rectangular Parallelepiped

WC—Worst Case

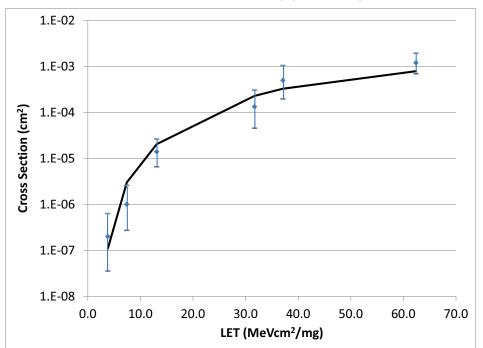
Outline



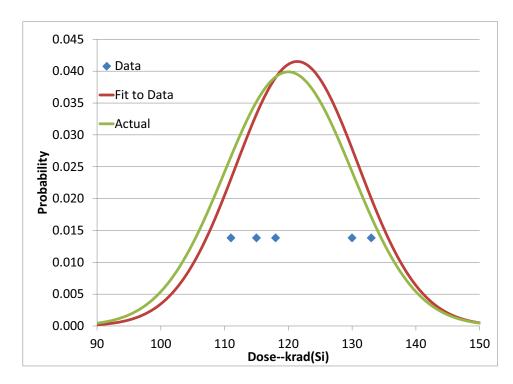
- Current RHA and It's Statistical Models
- II. Other Sources of Data and How They Are Used
- III. Bayesian Probability and Why It's Well Suited to RHA
- IV. Example: Bayesian SEE
- V. A More Complicated Example: Bayesian TID
- VI. Flight Heritage as data
- VII. Fitting data and Bounding rates in SEE
- VIII. Using Statistical Modelling to Meet Challenges of Destructive SEE
- IX. Conclusions

Radiation Hardness Assurance (RHA) Assumptions

- Single-Event Effect (SEE) Hardness Assurance Assumptions
 - Poisson errors on event counts dominate
 - Part-to-part and lot-to-lot variation in SEE response (usually) negligible
 - Destructive SEE (DSEE) may be exception
 - Charge collected defines SEE response
 - Mitigation: Large event counts minimize
 Poisson errors on cross sections
 - Rate constant; can happen any time



- Total Ionizing Dose (TID) Hardness Assurance Assumptions
 - Dominant errors from sampling due to part-to-part and lot-to-lot variation
 - Mitigation: Increase sample size and/or understand failure mechanisms and variation
 - Failures tend to cluster around mean failure dose



Radiation and Reliability



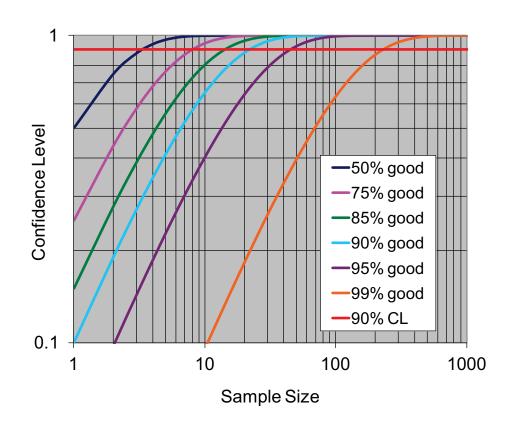
	How do radiation errors/failures compare to reliability issues?								
Q)	Failure Rate Decreasing	,	· · · · · · · · · · · · · · · · · · ·			Increasing Failure Rate; Failures Cluster			
Failure Rate	No Radiatio Analogue	Consta	F			TID Look Like This. Redundancy is ineffective.			
ш.—	Infant Mortality	SEE	Failure	s Indepen		orks./	Wearout		
	Useful Life (Failure Rate						Region Failure Rate		
	Decreasing)	ı	(Failure Rate Constant)			ı	Increasing	_	
0	1	2	3	4	5	6	7	8	
	Equivalent (accelerated + actual) Time (yrs) resented by Ray Ladbury at the Hardened Electronics and Radiation Technology (HEART) 2014 Conference, Huntsville, AL, March 17-21, 2014								

Presented by Ray Ladbury at the Hardened Electronics and Radiation Technology (HEART) 2014 Conference, Huntsville, AL, March 17-21, 2014 and published on radhome.gsfs.nasa.gov.

Current RHA and RHA Statistical Models



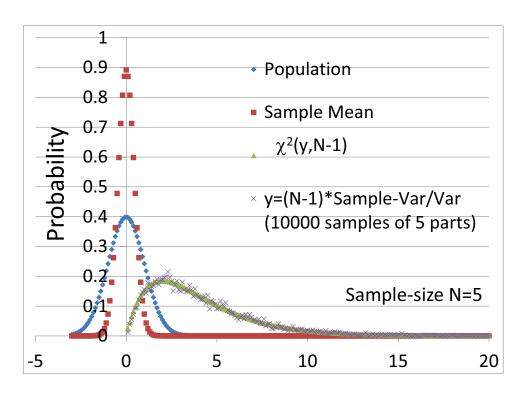
- Because radiation testing is destructive
 - test a sample representative of flight parts
 - use results to bound flight performance
- Least restrictive model is binomial
 - Assumes only that all parts from same distribution
 - Makes no assumptions about distribution of parts (failures, parametric changes, etc.)
 - Outcome is binary (Pass/Fail),
 - defines success probability, Ps and failure probability Pf=1-Ps
 - May be only choice when failure distribution highly uncertain
- Lack of guidance for derating and large sample size requirements provide incentive to adopt more restrictive model
 - Restrict population to a well behaved subset or "Lot"
 - Normal or Lognormal often assumed

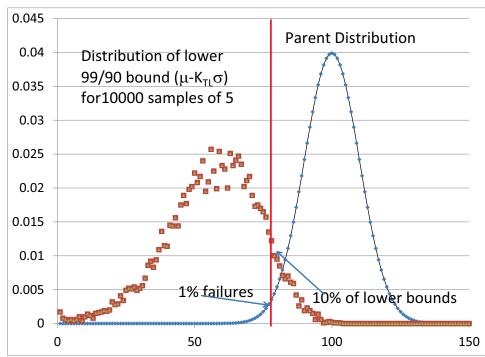


- Disadvantages of binomial sampling
 - No guidance on effectiveness of derating/increased margin
 - Requires large samples (e.g. 22 samples for Ps=90% @90% confidence level (CL))

Conventional model for TID RHA





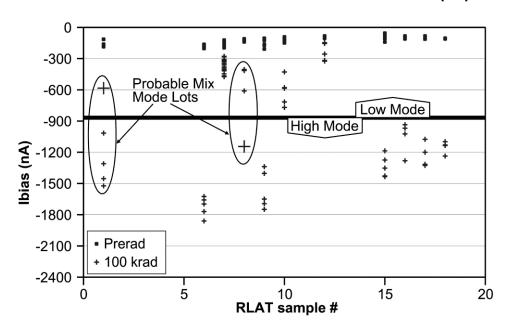


- Conventional TID RHA assumes "lot" is well behaved and unimodal
 - Wafer diffusion lot usually (not always) shows homogeneous performance
 - Assuming Normal distribution Sample mean and variance converge to population values rapidly
 - Can use one-sided tolerance limits—KTL(Ps,CL,n)—to bound performance and ensure success
 probability Ps with confidence CL for a test sample of size n

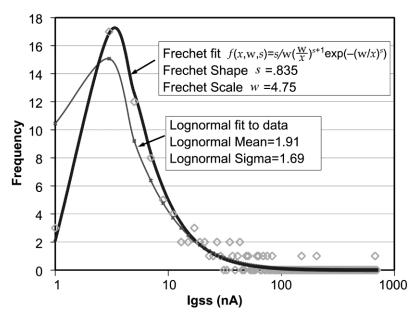
Distribution Pathologies do Occur



OP484 Ibias Prerad and 100 krad(Si)



NES 2N5019 After 1 Mrad(Si)



- Analog Devices (ADI) OP484 shows bimodal response even in same wafer lot
- Similar bimodal response seen in National Semiconductor LM111 (Kreig et al. NSREC 1999)
- Some devices show thick tails
- NES 2N5019 Junction Field Effect
 Transistor (JFET) showed high variation in IGSS after 0.3 and 1 Mrad(Si) (x-axis is logarithmic)
- ADI AD590 also shows thick tail

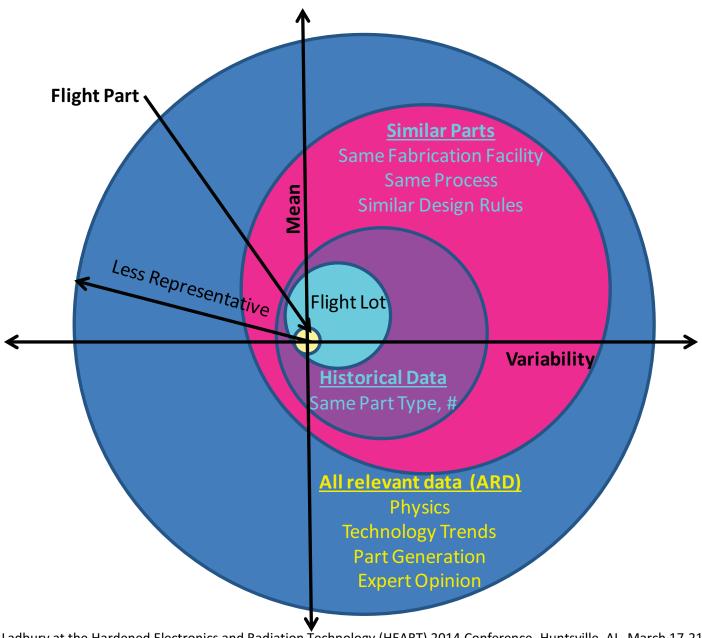
When There's No Lot-Specific Data



- Historical Data—Test data for the same part type/# as the flight parts, taken under similar application conditions
- Similarity/Process Data—Test data for parts with similar function fabricated at the same facility in the same process, taken under comparable application conditions
- Heritage Data—Data regarding past flight use of the same part type/#; heritage mission environments must usually be at least as severe as the current mission and application conditions must be comparable
- When you are really desperate
 - Physics—What do we know about the part and the radiation effects mechanisms that can place limits on their severity—example: Silicon-on-Insulator (SOI) limits SEE susceptibility
 - Technology trends—How have the susceptibilities changed over previous "similar" generations—e.g. SEL susceptibility for commercial SRAMs with minimum Complementary Metal Oxide Semiconductor (CMOS) feature size from 0.35 down to 0.11 microns
 - Technology generation—Susceptibility and trends thereof for comparable technologies from the same and even other vendors
 - Expert opinion—What do the smart kids think?
- None of these lines of evidence may restrict susceptibility in a meaningful way

Structure of Constraining Data

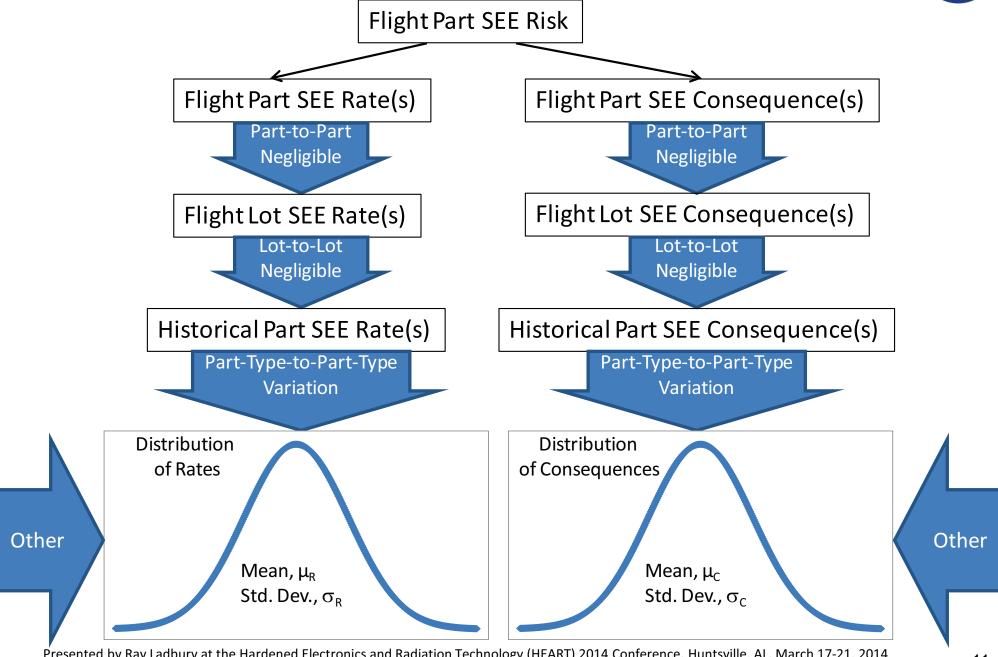




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SEE Risk Data Structure

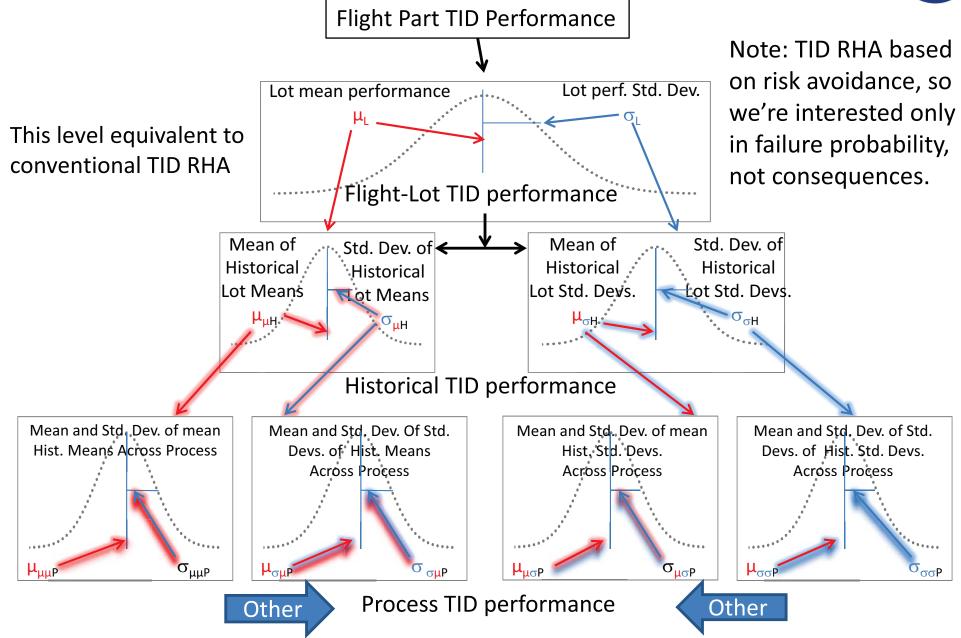




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Data Structure for TID RHA





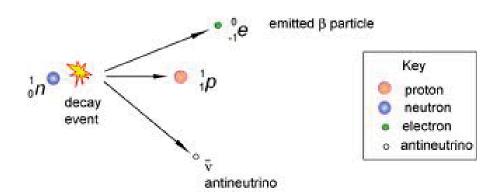
Two Types of Probability



- Physical probability
 - Indeterminacy is inherent in process;
 - no amount of additional data will change your odds for betting on outcome
- Subjective probability
 - indeterminacy reflects our limited knowledge
 - probability can change as our knowledge increases
- Analogues to RHA
 - Probability of observing an SEE for a particular ion is physical
 - Probability our lot has a majority of parts that will meet mission requirements is subjective

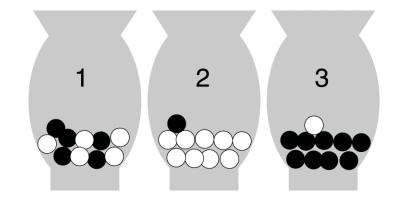
Physical (or Objective) Probability

Beta Decay of a Neutron



Subjective Probability

$$P_{123}(S)=0.5$$



Bayes' Theorem



Bayes Theorem:

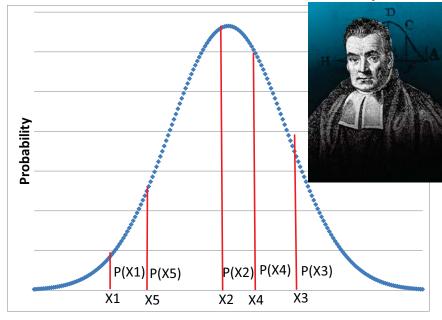
$$\begin{split} P(Model \mid Data) &= \frac{P_{pr}(Model)P(Data|Model)}{\sum\limits_{Models}P_{pr}(Model)P(Data|Model)} \\ &- P_{pr}(Model) = Prior \ is \ probability \ of \ our \end{split}$$

- model before we consider new data
- P(Model|Data) is updated (posterior) probability—the probability that takes into account data AND prior expectations
- Denominator ensures normalization, but is also a measure of probability for all models
- Bayesian probabilities are subjective
 - Depend on our knowledge at the time of calculation
 - Can change as we add new knowledge
 - May be associated with a "confidence"
- Bayes Theorem is the most efficient way to update probabilities given new data

P(Data|Model) is likelihood, L

L=P(X1)*P(X2)*P(X3)*P(X4)*P(X5)

Thomas Bayes



Data {X1,...X5] drawn at random. Candidate model is P(X) above.

Bayesian Approach to RHA



Previous Test Data

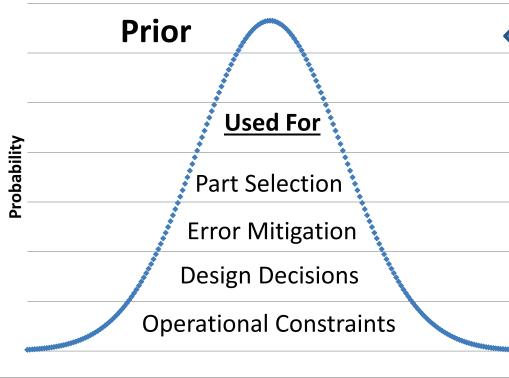


Data for Similar Parts

1)Must relate input data to SEE/TID failure rates or consequences

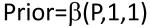
2)Input data must produce fairly compact, well behaved distributions

Physics, **Expert Opinion** Heritage Etc. **PRIOROMATIC**



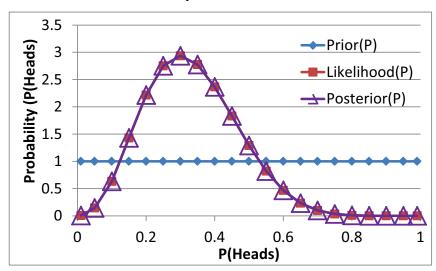
Effect of Prior and Likelihood

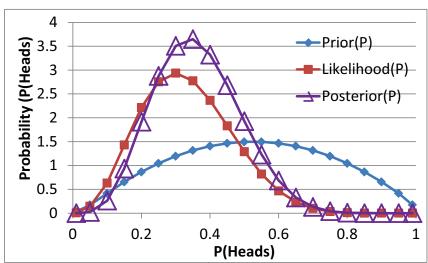




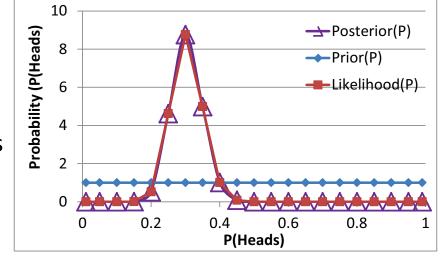
Prior= β (P,2,2)

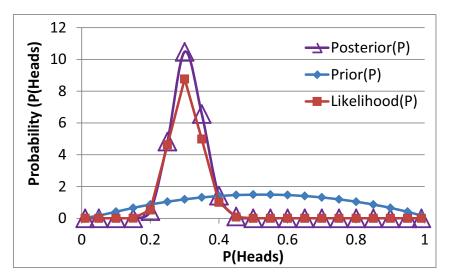






30 Heads In 100 Tosses





Probability (P(Heads)) for different Priors as data increases

Minimizing Subjectivity



- Uninformative Priors—Broad, slowly varying (flat) Priors give rise to Posterior distributions that reflect the data (likelihood)
 - If Prior is 0 anywhere, Posterior also 0 there (impossible means impossible)
 - Some Uninformative priors (for discrete distributions) are called Maximum Entropy priors
- Empirical Bayes allows looking at the data before developing Prior
 - Can locate Prior at the maximum of the likelihood and make it very broad
 - This means you think the likelihood probably gives the best guess for the best fit, but allow for significant sampling error
 - Usually yields good results unless there are serious sampling or systematic errors
 - Some Bayesians refer to this as "cheating"
- Maximize the data to update the Prior and dilute its influence.
- Also, you don't have to try only a single Prior—you could even attach prior
 probabilities to your priors if you want to go really meta. Or you could try
 several Priors just to gauge the dependence of results on the Prior.

Data Sources



Table I: SET Data for ADI and Linear Technology (LTC) Op Amp

		SET Rate	WC	WC	
	Vendor/ Process	(day ⁻¹)	duration	amplitude	Supply—Output
RH108[2]	LTC—RH Bipolar	0.011	7 μs	4.5 V	0/12V—6V
RH118[2]	LTCRH Bipolar	0.046	>5 μs	2 V	-8V/+8V—0V
RH1014[2]	LTCRH Bipolar	0.029	>35 µs	rail-to-rail	-12V/+12V—6V
RH1499[3]	LTCRH Bipolar	0.0082	13 μs	4.4 V	-15V/+15V—4V
RH1078[4]	LTCRH Bipolar	0.04	30 μs	2 V	0/10V-2V
OP27[5]	ADI—Bipolar>2.5 μm	0.036	10 μs	10V	-10V/+10V — varied
OP113[2]	ADI — Bipolar>2.5 μm	0.01	>2 µs	1.7 V	0/5V-2.55V
OP270[2]	ADI — Bipolar>2.5 μm	0.35	1.2 μs	3 V	-5V/+5V — 0.42V
OP400[2]	ADI — Bipolar>2.5 μm	0.56	10 μs	3 V	-12V/+12V —±2.4V
OP05[5]	ADI — Bipolar>2.5 μm		12 μs		
OP15[5]	ADI — Bipolar>2.5 μm		15 μs		

Single-event transients (SETs) depend on application conditions. Data here correspond to worst-case transients for the device. Worst-case SET rate and duration can be modeled as lognoral distributions for op amps across the ADI bipolar>2.5 micron and LTC RH process. WC amplitude can be modeled as a beta distribution, but assuming rail-to-rail transients is not overly conservative.

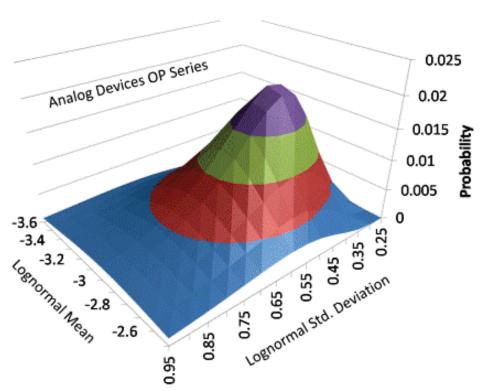
TABLE II: SEL DATA FOR ADI 0.6 μM CMOS ADCS AND DACS

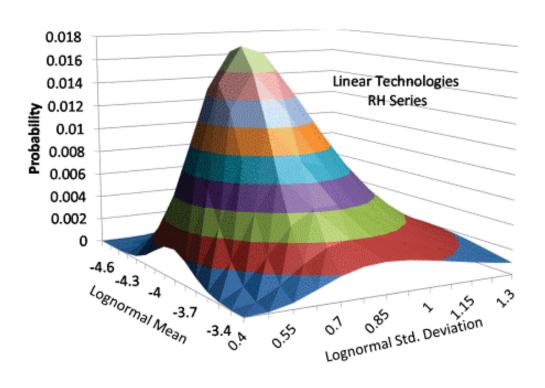
Part #	Process	Onset LET (MeVcm2/mg)	Test Facility	σ _{lim} (cm²)
AD5305	0.6 um	LET<11	BNL	??
AD7472	0.6 um	11 <let<15< td=""><td>BNL</td><td>5.00E-04</td></let<15<>	BNL	5.00E-04
AD7476	0.6 um	LET<60	BNL	??
AD7664	0.6 um	6	BNL	2.50E-04
AD7714	0.6 um	15 <let<24< td=""><td>BNL</td><td>6.00E-04</td></let<24<>	BNL	6.00E-04
AD9260	0.6 um	8	BNL	35
AD5334	0.6 um	5	TAMU	5.00E-04
AD7664	0.6 um	4	TAMU	1.00E-03
AD7675	0.6 um	4	TAMU	3.00E-05
AD7714	0.6 um	20 <let<22< td=""><td>TAMU</td><td>1.00E-04</td></let<22<>	TAMU	1.00E-04

SEL saturated cross sections vary too widely to model SEL rate as a compact distribution. Onset Linear Energy Transfer (LET) appears to be bimodal, but we can model the lower mode as a lognormal to determine worst case (WC) onset LET for SEL in a process at a given confidence level.

Single-Event Transient (SET) Rate Priors





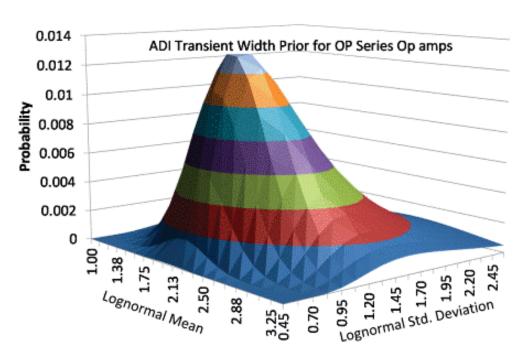


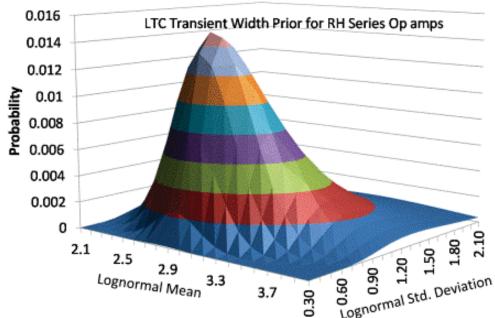
SETs rates for ADI OP series bipolar feature size>2.5 μ m op amps are distributed roughly lognormally across the family with lognormal mean=-3 and standard deviation=0.45. The 90% softest part would have ~0.089 SETs/day, or with 90% confidence <0.19 SETs/day.

The best-fit lognormal to SET rates across LTC RH Series op amps had lognormal mean=-3.8 and lognormal standard deviation= 0.65. The 90% softest part would show ~0.027 SETs/day or with 90% confidence <0.13 SETs/day.

SET Duration Priors







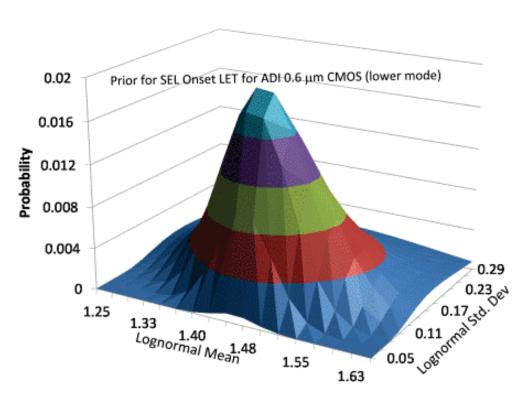
SET durations in ADI and LTC op amps can also be modeled as a lognormal, yielding best fit mean and standard deviation and the results used to bound SET duration to any desired confidence level (See Table III.) These results can be used to select parts or for purposes of filtering transients in a design

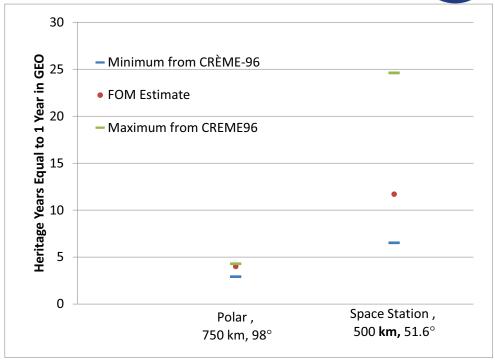
TABLE III: BOUNDING SET WIDTHS FOR ADI AND LTC OP AMPS

Process	Typical	90% WC	Typical@90% CL	90%WC@90%CL
ADI	15 µs	<35 μs	143 µs	<218 μs
LTC	22 µs	<35 μs	75 μs	<170 μs

SEL Onset and Heritage







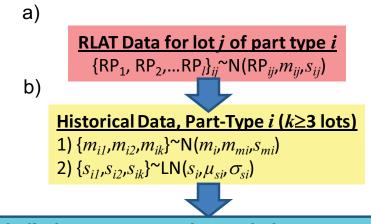
SEL cross sections vary too much across parts in a process to model rates. However, onset LET for SEL for ADI's 0.6 μ m CMOS ADCs and DACs seems to fall into two compact modes. To bound the onset LET, we model the lower mode as a lognormal. With 90% confidence, onset LET for parts in this process should be >2.7 Mev-cm²/mg.

Heritage is often proposed en lieu of testing to qualify a component/system. If heritage environment differs from mission environment, each heritage year can be weighted by the ratio of the heritage SEE rate to the mission SEE rate. However, this ratio depends strongly on device geometry if the heritage and mission environment

TID Degradation of Bipolar Junction Transistor (BJT) Gain



- Rad. Performance (RP=Gain(Prerad)/Gain(Postrad)) for every part (1<RP)
- Part-to-part variation: Each lot has a mean and a standard deviation, usually determined by Radiation Lot Acceptance Test (RLAT)
- Lot-to-lot variation: Look at how lot means and standard deviations vary
 - A lognormal distributions of means with a lognormal mean and standard deviation
 - Lognormal distribution of standard deviations (two parameters)
- Part-type-to-part-type: each lot-to-lot parameter now a distribution
 - 8 parameters describing part-to-part, lot-to-lot and part-type-to-part-type variation



c)

Similarity Data summarizes variation over part types

 $\{m_{mi}\}\sim N(m_m, m_{mm}, s_{mm})$ =Variation of avg. m_m over part types $\{\mu_{si}\}\sim N(\mu_s, m_{\mu s}, s_{\mu m})$ =Variation of avg. s_{μ} over part types $\{s_{mi}\}\sim LN(s_m, \mu_{sm}, \sigma_{sm})$ =Variation of avg. s_m over part types $\{\sigma_{si}\}\sim LN(\sigma_{s}, \mu_{\sigma s}, \sigma_{\sigma s})$ =Variation of avg. σ_{s} over part types

a) Variability of radiation performance (RP) for a lot j of part type i is assumed to follow a Normal distribution (N) with mean m_{ij} and standard deviation s_{ij} . b) We summarize variability across lots for part type i by fitting the lot means to a Normal distribution with m_{mi} and s_{mi} as parameters and the standard deviations to a lognormal (LN) with parameters μ_{si} and σ_{si} , since standard deviations are positive definite. c) Likewise, we can summarize variability over similar part types in the same process by fitting the historical parameters to Normal or lognormal distributions as indicated.

Prior Distributions for Variability in Semicoa NPNs



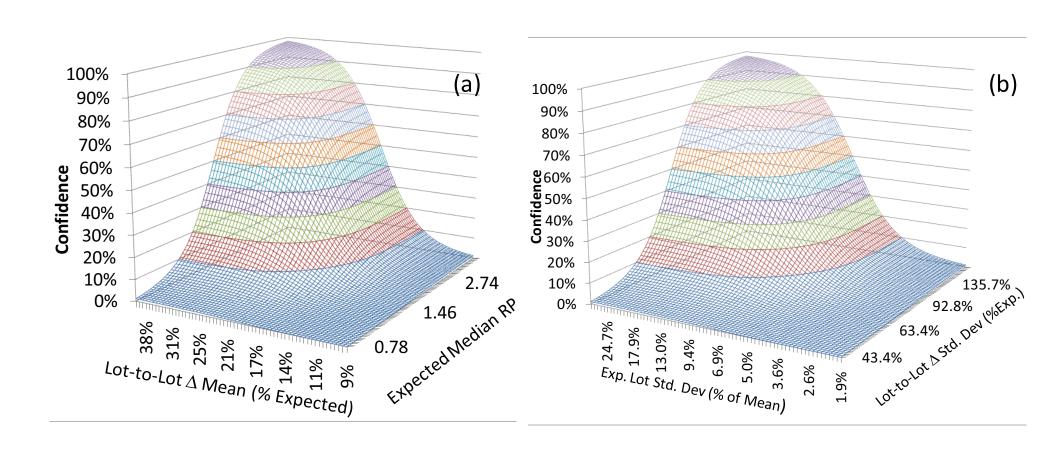


Fig. 3. Prior probability distributions summarize (a) the expected gain degradation and the standard deviation about that mean for an arbitrary Semicoa NPN BJT as well as (b) the variability of those quantities from lot to lot.

Prior Distributions for Variability in MS-L PNPs

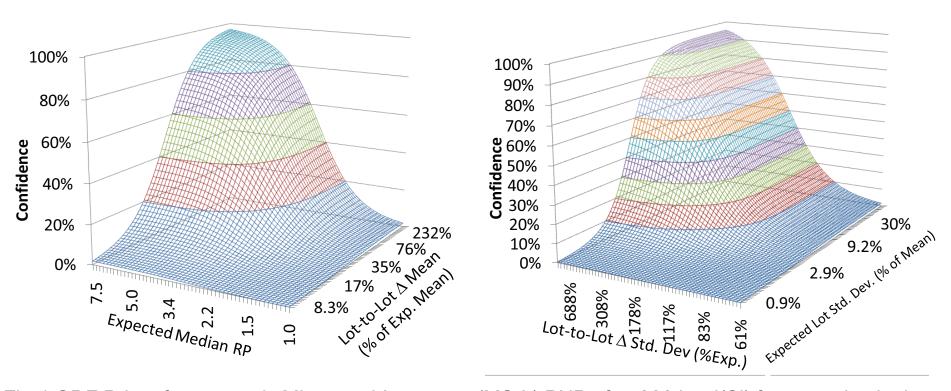


Fig.4 GDF Priors for a generic Microsemi-Lawrence (MS-L) PNP after 300 krad(Si) for operation in the "middle" of the device's current range. Despite the fact that the transistors for the Prior have different voltage and current characteristics, the Priors place meaningful constraints on expected gain degradation. However, lot-to-lot variation is less well constrained, especially for part-to-part standard deviation.

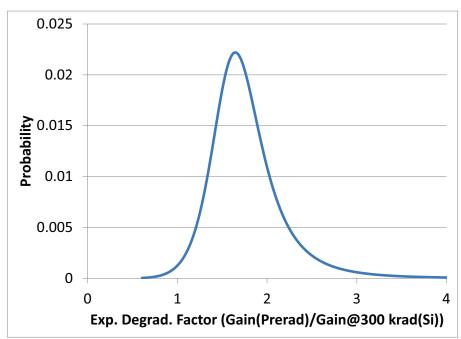
What If There's No Data to Update Priors?



- Consider probability distribution for expected mean degradation
 - Have $P(m_m, m_{mm}, s_{mm})$ and $P_{mm}(m_{mm}, s_{mm})$
 - Can select most probable value of m_{mm} and s_{mm} based on $P_{mm}(m_{mm}, s_{mm})$
 - Alternatively, can treat m_{mm} and s_{mm} as nuisance variables and integrate over them to find an average or expected probability distribution for $P(m_m)$ —the expected mean for a generic mean degradation of a generic transistor type in this process

$$\langle P(m_m) \rangle = \int P(m_m, m_{mm}, s_{mm}) P_{mm}(m_{mm}, s_{mm}) dm_{mm} ds_{mm}$$

 Similar operations possible for all lot-to-lot parameters and can be repeated to yield expected degradation for a generic xster in a generic lot for a generic xster in process



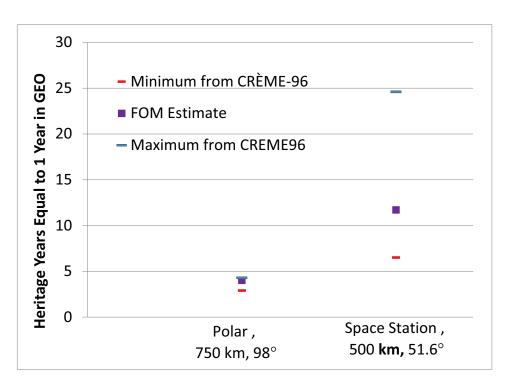
Over 90% of PNP xstrs from MS-Lawrence would have mean lot gain degradation factor<2.1.

Repeating for other parameters: Gain of the 99% WC part from the the 90% WCPNP in the MS-L process should degrade <3x after 300 krad(Si).

It's Not Bayesian if You Don't Update the Prior



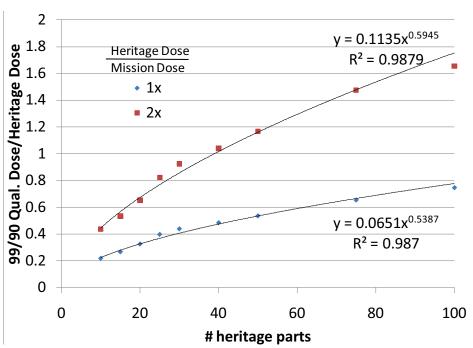
- For SEE, weight of heritage mission depends on environment
 - 1st order: Ratio of Figure-of-Merit coefficients in heritage and mission environments
 - Also depends on details of charge collection volume in device—and difference can be much larger if heritage and mission radiation environments differ dramatically



- Without test data, must update Prior w/ heritage data
- For TID, we only know mission i parts worked after exposure to dose D_i

$$L = \prod_{i=1}^{n} (1 - P(D_i))$$

- D_i 's must be lower bounds



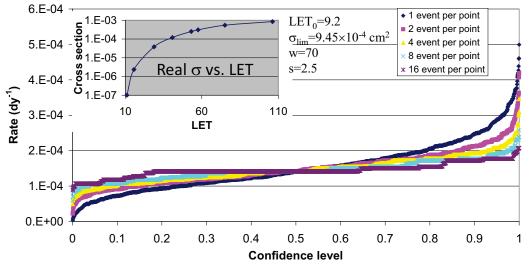
Fitting SEE Data



- For small event counts, use fit that considers Poisson errors
- Generalized linear model:

$$\begin{split} L &= \prod_{i=1}^{n} Poisson(n_{i}^{obs}, \mu_{i}) \\ \mu_{i} &= \sigma_{sat} \times Weibull(LET_{i} - LET0, W, s) \end{split}$$

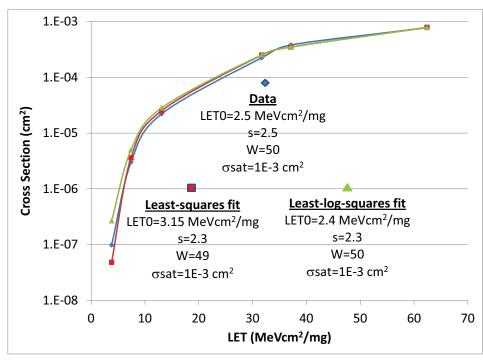
- Solve for osat, LETO, W and s that give best fit or WC rate at desired confidence level
- Can use any model to predict μ_i



- If Poisson errors negligible, use exact fit
- Least squares not optimal @ low LET
- Least log-squares (LLS) may be better

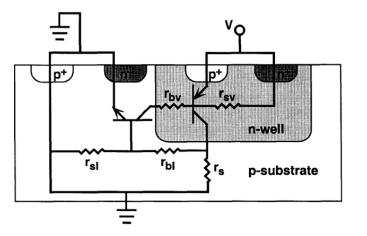
$$LLS = \sum_{i=1}^{n} F_{i}^{pred} \times (logF_{i}^{pred} - logF_{i}^{obs})^{2}$$

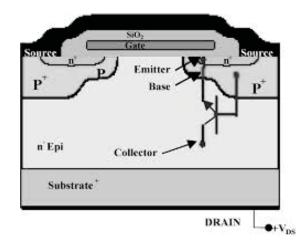
LLS gives better fit near-threshold

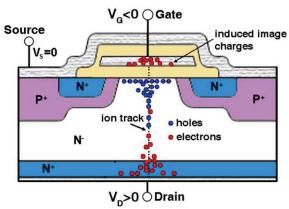


Statistical Models for Destructive SEE









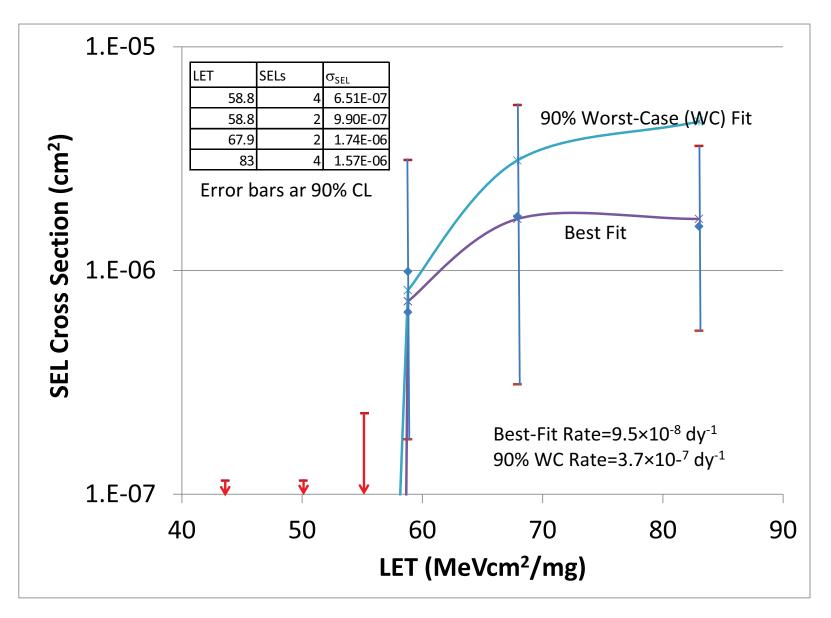
- Single-event latchup (SEL)
 - -parasitic bipolar effect in CMOS
 - –Can sometimes get several SELs per device before failure
 - –Recovery very disruptive
 - -Also seen at cryogenic temp.
 - Latent damage possible
- Rate estimation trouble:
- poor statistics
- Dataset may include many devices w/ varying susceptibility
- depends on Energy + LET

- Single-event burnout (SEB)
 - parasitic bipolar effect
 - Similar events seen in FLASH, bipolar ICs, Schottky diodes
 - Can get several SEBs per device for discrete xstrs, but not for other device types
- Rate estimation difficult:
- poor statistics
- Dataset may include many devices w/ varying susceptibility
- Complicated dependence on energy, angle and ion species

- Single-event Gate Rupture (SEGR) depends on gate oxide and charge transport
 - –Always destructive
 - -Precursor events damage oxide
 - –Single-event dielectric rupture (SEDR) somewhat analogous
- Rate est. complicated by
- poor statistics
- Dataset may include many devices w/ varying susceptibility
- Complicated dependence on energy, angle and ion species

GLM Approach Applied to LTC RAD1419





Can estimate rate for a given confidence if statistics adequate for each part.

Limitations of GLM for Destructive SEE

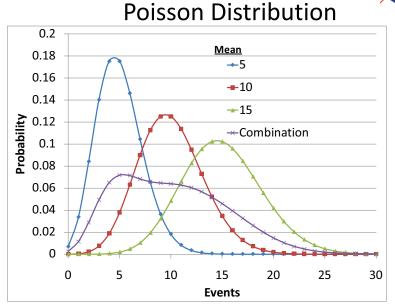


- GLM technique works well when statistics accumulated for each test device
 - Allows bounding of rate for a given confidence level
 - Flexible and can be adapted to include other sources of error
 - Model need not be standard Weibull rectangular parallelepiped
 - Could even be Monte Carlo output for several geometric models of sensitive volume
- Unfortunately, for some device types, every event kills a part
 - SEGR is always destructive to power Metal-Oxide-Semiconductor Field Effect
 Transistor (MOSFET) as are failures in FLASH, bipolar microcircuits and diodes
 - Accumulating statistics done over several parts
 - How do you detect/treat part-to-part variation
- Even if statistics gathered for each device, susceptibility can change w/ time
 - TID can alter susceptibility
 - Latent damage due to overcurrent (SEL, SEB, etc.) or bus contention due to SEE
 - Complex devices may have different susceptibilities during different
- How do we deal with Poisson error, part-to-part variation and time dependent susceptibility—possibly all at the same time?

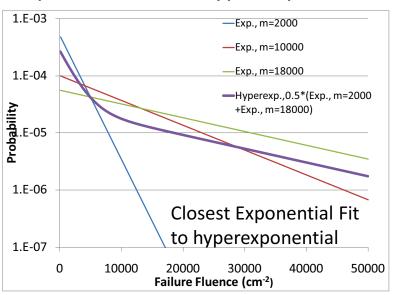
What Can We Tell form Statistics of DSEE?

NASA

- Poisson DSEE→ Failure fluence, F_{FAIL} follows exponential distribution
 - Variability insignificant →single mean for all parts, so F_{FAIL} follows single exponential
 - Significant variation → F_{FAIL} follows mixture of exponentials, or hyperexponential distribution
 - Hidden Markov process— F_{FAIL} distribution depends on part selected
- Compare distributions characteristics of F_{FAIL} across parts
 - Mean/Std. Deviation, skew, kurtosis, Range
 - For details, see presentation from 2012
 SEE Symposium, "Assessing Part-to-Part
 Variation for Destructive Single-Event
 Effects"



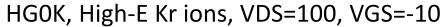
Exponential and Hyperexponential

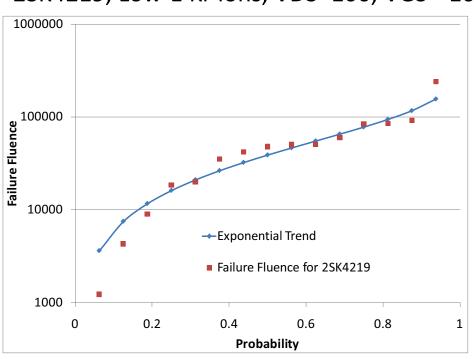


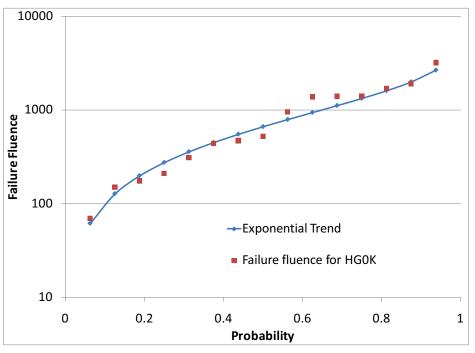
Detecting variability in MOSFETs*



2SK4219, Low-E Kr ions, VDS=100, VGS=-10







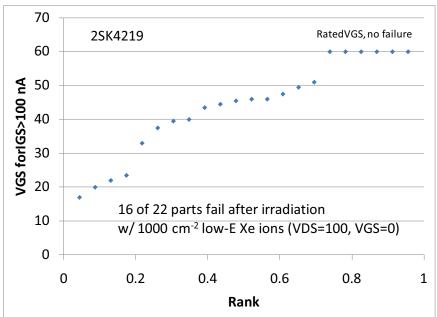
- 2SK4219 MOSFET shows more failures at low fluence than expected for exponential
 - Comparison of distribution characteristics: mean/Std. Dev, skew, range, kurtosis
 - Shows 6% probability of purely exponential behavior
- F_{FAIL} for HG0K MOSFET shows better fit to exponential
 - Comparison of distribution characteristics shows significance only at 71% level

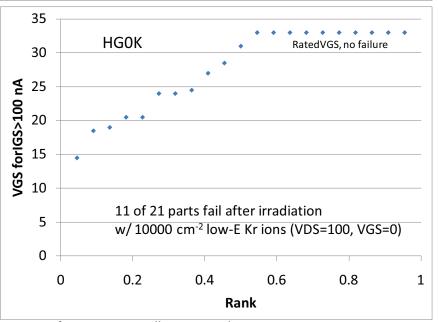
^{*}Data courtesy of Veronique Ferlet-Cavrois, See IEEE TNS vol. 59, pp. 2920-2929

For MOSFETS Failing During PIGS Test



- Often for VGS=0, MOSFETs do not fail during irradiation, but during Post-Irradiation Gate Stress (PIGS) test
 - Evidence of latent damage, and failure imminent
- F_{FAIL} unknown, but can be estimated if some but not all parts fail at fluence F
 - Assume failure probability binomial
 - $P_{FAIL}^N_{FAIL}/N_{TEST}^1-exp(-F/\langle F \rangle)$
 - For 2SK4219, $\langle F_{Fail} \rangle$ ~3140 cm⁻², w/ 90% CL from 1599 to 5735 Xe ions per cm²
 - For HG0K, $\langle F_{Fail} \rangle$ ~15500 cm⁻², w/ 90% CL from 9000 to 25000 Kr ions per cm²
 - Note that this is not necessarily the same as the SEGR $\langle F \rangle$





If We Can Model Fluence to Failure



• Assuming we accumulate m_i events at LET_i, (example model: RPP Weibull)

$$\mathcal{L} = \prod_{i=1}^{n} \prod_{j=1}^{m_i} 1/F_i(LET_i) \exp(-F_i/F_i(LET_i), F_i(LET_i) = 1/\sigma_{lim} \times \left[Weibull(LET-LET_0, W, s]\right]$$

- Initially assume F_i the same for each event j accumulated for LET_i,
 - Compare likelihood for each LET—a dramatically poor fit may indicate that expected fluence to failure has changed from event to event
 - May be due to multiple parts, latent damage, change in vulnerability due to new operation...
 - Can introduce models of variability to better match results given enough data.
- Models for F_{Fail} much more complicated for
 - SEL—F_{Fail}(LET,Range)
 - SEGR and SEB—F_{Fail}(Z,Energy,Angle)
 - May be possible to simplify radiation environment in terms of Equivalent LET
 - F_{Fail} could be mean values of F_{Fail} for Monte Carlo simulations done over different candidate models of the sensitive volume

Conclusions



- Statistical models are inherent to current RHA methods; some examples:
 - Use of one-sided tolerance limits for TID
 - Guidance for event counts in SEE testing
- Models to date tend to concentrate on "ideal" or most representative data
 - Assumption that TID performance in a wafer lot follows well behaved distribution
 - Assumption that part-to-part and lot-to-lot variation of SEE response is negligible
 - SEE counts sufficiently high that Poisson errors don't affect SEE rates
- Much more data less than ideal (similarity, heritage, historical...)
 - Often used for a "warm fuzzy"
 - Bayesian methods here allow quantitative bounds to be placed on radiation response
- Statistical techniques very promising for bounding destructive SEE
 - May be very important if commercial hardware being used
 - Destructive SEE must be rare, or hardware will not meet requirements
 - Rare events are inherently difficult to bound
- Proper use of statistics essential for reliable economical space systems
 - Any fool can lie with statistics—Experts use them to expose the truth